

Time: 15 minutes.

1. The variable names x and y stand for arbitrary integers. Which of the following statements are true, and false, respectively? Why?
 - $P_1 : \forall x \forall y: x^2 + y = 10.$
 - $P_2 : \forall y \forall x: x^2 + y = 10.$
 - $P_3 : \exists x \exists y$ such that $x^2 + y = 10.$
 - $P_4 : \exists y \exists x$ such that $x^2 + y = 10.$
 - $P_5 : \forall x \exists y$ such that $x^2 + y = 10.$
 - $P_6 : \forall y \exists x$ such that $x^2 + y = 10.$
 - $P_7 : \exists x$ such that $\forall y: x^2 + y = 10.$
 - $P_8 : \exists y$ such that $\forall x: x^2 + y = 10.$
2. Are there pairs among the statements above that are equivalent? Why?
3. Negate statements P_1 , P_4 and P_7 .