

Problem 1 Let $A = \{1, 3, 4, 7, 8\}$ and $B = \{2, 4, 3, 6, 9\}$. Find $A \cup B$, $A \cap B$, $B \setminus A$.

Problem 2 Show: $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$.

Problem 3 Show: If $A \cup B = B$, then $A \subseteq B$.

Problem 4 1. Show: $(A \cap B)^c = A^c \cup B^c$.

2. State the corresponding result in propositional logic.

Problem 5 Find $\bigcap_{n \in \mathbb{N}} \left[0, 1 + \frac{1}{n}\right] = [0, 2] \cap \left[0, 1 + \frac{1}{2}\right] \cap \left[0, 1 + \frac{1}{3}\right] \cap \dots$

Problem 6 Find $\bigcap_{n \in \mathbb{N}} \left[1, 1 + \frac{1}{n}\right]$.

Problem 7 Find $\bigcap_{n \in \mathbb{N}} \left(1, 1 + \frac{1}{n}\right)$.

Problem 8 1. Show $\bigcup_{n \in \mathbb{N}} (A_n)^c \subseteq \left(\bigcap_{n \in \mathbb{N}} A_n\right)^c$.

2. Show $\left(\bigcap_{n \in \mathbb{N}} A_n\right)^c \subseteq \bigcup_{n \in \mathbb{N}} (A_n)^c$.