

Curl and Rotation

Math 3335

Helmut Knaust - Department of Mathematical Sciences, University of Texas at El Paso,

hknaust@utep.edu

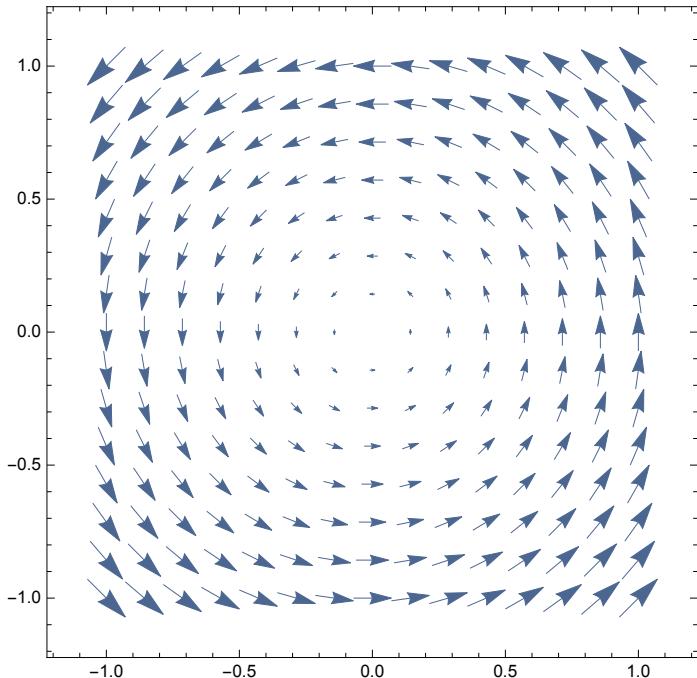
10/27/16

|

```
f[x_, y_] = {-y, x}
```

```
VectorPlot[f[x, y], {x, -1, 1}, {y, -1, 1}]
```

```
{-y, x}
```

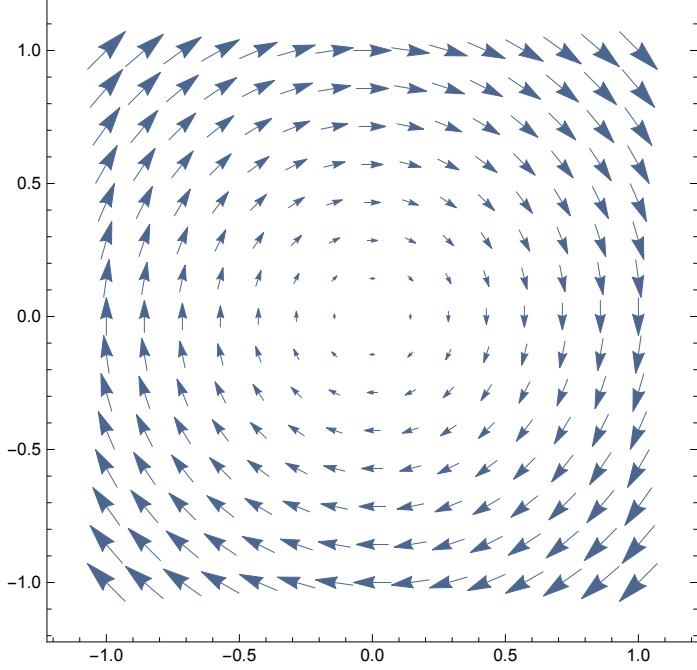


```
Curl[f[x, y], {x, y}]
```

2

2

```
f[x_, y_] = {y, -x}
VectorPlot[f[x, y], {x, -1, 1}, {y, -1, 1}]
```

{ $y, -x$ }

```
Curl[f[x, y], {x, y}]
```

-2

3

```
f[x_, y_] = {y, -x} / (x^2 + y^2)
VectorPlot[f[x, y], {x, -1, 1}, {y, -1, 1}];
```

$$\left\{ \frac{y}{x^2 + y^2}, -\frac{x}{x^2 + y^2} \right\}$$

```
Curl[f[x, y], {x, y}]
```

$$\frac{2x^2}{(x^2 + y^2)^2} - \frac{2}{x^2 + y^2} + \frac{2y^2}{(x^2 + y^2)^2}$$

```
Simplify[%, Assumptions → Not[{x, y} == {0, 0}]]
```

0