

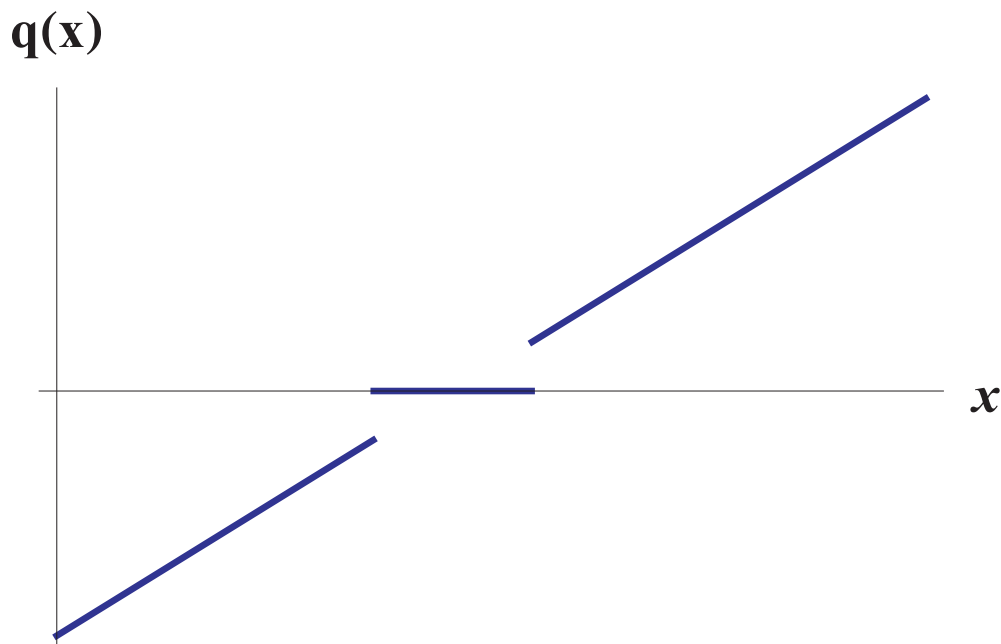
The most basic quantization technique is **Thresholding**:

Given a signal  $\vec{x} = (x_i)$  and a single threshold  $\sigma$ , we replace values as follows:

$$q(x_i) = \begin{cases} 0 & \text{if } |x_i| \leq \sigma \\ x_i & \text{if } |x_i| > \sigma \end{cases}$$



The thresholding quantization function:



## The JPEG2000 Quantization Scheme

The **Lossy JPEG2000 Quantization Scheme** also has one fixed parameter,  $\tau$ . After wavelet transformation, a “step” quantization

$$q(x_i) = \text{sgn}(x_i) \cdot \sigma \cdot \left\lfloor \frac{|x_i|}{\sigma} \right\rfloor$$

is applied to each region with a parameter  $\sigma$  determined as follows:

$\frac{\tau}{2}$	$\tau$
$\tau$	$2\tau$

$n = 1$



## The JPEG2000 Quantization Scheme

The **Lossy JPEG2000 Quantization Scheme** also has one fixed parameter,  $\tau$ . After wavelet transformation, a “step” quantization

$$q(x_i) = \text{sgn}(x_i) \cdot \sigma \cdot \left\lfloor \frac{|x_i|}{\sigma} \right\rfloor$$

is applied to each region with a parameter  $\sigma$  determined as follows:

$\frac{\tau}{4}$	$\frac{\tau}{2}$	$\tau$
$\frac{\tau}{2}$	$\tau$	
$\tau$		$2\tau$

$$n = 2$$



January 6-9 | New Orleans, LA  
2011 Joint Mathematics Meetings

## The JPEG2000 Quantization Scheme

The **Lossy JPEG2000 Quantization Scheme** also has one fixed parameter,  $\tau$ . After wavelet transformation, a “step” quantization

$$q(x_i) = \text{sgn}(x_i) \cdot \sigma \cdot \left\lfloor \frac{|x_i|}{\sigma} \right\rfloor$$

is applied to each region with a parameter  $\sigma$  determined as follows:

$\frac{\tau}{8}$	$\frac{\tau}{4}$	$\frac{\tau}{2}$	$\tau$
$\frac{\tau}{4}$	$\frac{\tau}{2}$		
$\frac{\tau}{2}$	$\tau$		
$\tau$	$2\tau$		

$$n = 3$$



January 6-9 | New Orleans, LA  
2011 Joint Mathematics Meetings

The quantization function for a given region:

